

Fig. 3 Amplitude decay of cone model mounted to flexure C.

The reason for the obviously low damping derivatives will be investigated further. It is intended to investigate the effects of nose bluntness, oscillation amplitudes, and frequencies on the damping. A quasi-steady analysis is planned, based on the experimentally determined normal force distribution along the model. The investigation will be extended to various trim angles of attack.

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Approximate Payload Capabilities of Boosters for Planetary Missions

ALAN B. BAKER*

Radio Corporation of America, Princeton, N. J.

Nomenclature

- E = injection energy, joules
 g = gravitational constant, 9.81 m/sec²
 I_{spj} = specific impulse of the j th stage, sec
 m_1 = escape mass, kg
 n = number of booster stages
 P = weight of payload, lb
 R = radius of Earth, 6.38 (10⁶) m
 r_0 = parking orbit radius, 6.57(10⁶) m
 W_{ij} = weight of vehicle at beginning of j th stage, lb
 W_{fj} = weight of vehicle at end of j th stage, lb
 V = actual terminal velocity at injection, m/sec
 V_L = velocity loss because of drag and gravity, 1524 m/sec (5 kft/sec)

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* Associate Engineer, Astro-Electronics Division.

THE payload capability of any chemical booster depends primarily on its ascent trajectory and the injection energy required for the particular mission. At the end of the ascent phase, the spacecraft must have a final velocity and orientation to permit escape from the earth's gravitational field and to rendezvous, at the proper time and place, with the target planet. There are two alternative ascent paths: a direct-ascent trajectory, where the booster stages burn successively, with only short coast periods to permit separation of the stages; and a parking-orbit trajectory, where the burning time is divided into two periods, separated by a coasting interval in a circular orbit. The parking-orbit trajectory is much preferred to the direct ascent, although the latter has shorter flight time.² The major disadvantage of the latter is that it must satisfy both the energy requirements and the geometrical constraints simultaneously, which results in a narrow launch window, an inefficient ascent path, and a loss in payload capability. Parking orbit trajectories permit higher payloads and more flexibility in launching time because the in-orbit time and launch azimuth can be varied for the same mission. The lowest possible parking-orbit altitude permits the greatest payload capability, and this capability decreases as the altitude is increased. A 100-naut-mile parking orbit ascent trajectory was assumed in all calculations.

The optimum type-I transfer characteristics for the planets under consideration are listed in Table 1, abstracted from Clarke's tables.¹ These optimum conditions are cyclic and each occurs once during the planet's metonic cycle.† Mars' metonic cycle is 15 yr. The characteristics for the period listed for Mars will repeat for the period 1977 through 1992. No transfer characteristics are listed for Venus beyond 1970, since its metonic cycle is ~8 yr; the conditions listed will repeat for the period 1970 through 1978 and again during 1978 through 1986. Jupiter's metonic cycle is ~12 yr, but because of its nearly circular orbit and relatively large distance from Earth, there is very little variation in these characteristics from year to year—the required geocentric injection energy ranges from 0.77(10⁸) to 1.1(10⁸) m²/sec² for 1968 through 1973, and launch windows occur every 13 months. Mercury's metonic cycle is ~1 yr; hence, the conditions shown occur annually.

Geocentric injection energy is the vehicle's remaining kinetic energy after it escapes from the Earth's gravitational field. It is independent of the heliocentric flight path and is defined by the equation

$$E = \frac{1}{2}m_1V^2 - gR^2m_1/r_0 \quad (1)$$

or

$$2E/m_1 = V^2 - 1.216(10^8) \quad (2)$$

Values of $2E/m_1$ are tabulated in Table 1.

It is theoretically possible to travel from Earth to a planet on several different ballistic paths at any given moment, but only a small number of these paths have a sufficiently low injection energy requirement to be usable with currently available or planned boosters. Of these, the most practical paths are those that require less than one revolution about the sun. Type I trajectories make less than one-half of one revolution about the sun and type II trajectories make between one-half and one revolution around the sun. Within each type there are two possible trajectories, class I and class II. Class I has a smaller heliocentric central angle and hence a shorter flight time than class II.³

The value of $2E/m_1$ listed in Table 1 for a particular launch period is the greatest value that might be required to launch the vehicle at any time within that period. The launch date requiring the minimum energy occurs at some time within the smallest launch interval. These listings show that a

† The period of cyclic occurrence of the same absolute fixed geometry between Earth and the planet. The length of this cycle depends on the planet's orbital velocity relative to Earth.

Table 1 Type I transfer characteristics^a

Launch dates	t_L , days	$2E/m_1$, $\frac{m^2(10^8)}{sec^2}$	Class I trajectories				Class II trajectories			
			t_F , days	S_{com} , 10^6 km	V_{hxs} , km/sec	δ_g , deg	t_F , days	S_{com} , 10^6 km	V_{hxs} , km/sec	δ_g , deg
MARS										
10/23/62-11/7/62	15	0.1612	206/224	214/244	4.03/5.24	40.2/45.7	235/260	242/281	2.88/4.11	45.4/54.8
10/18/62-11/17/62	30	0.1821	188/288	193/313	2.55/6.30	21.3/49.1	224/292	221/315	2.53/4.88	6.6/61.5
10/11/62-11/25/62	45	0.232	163/279	167/312	2.66/7.94	23.3/46.1	221/294	208/320	2.80/5.40	-5.2/70.4
11/12/64-11/27/64	15	0.094	233/246	214/225	4.05/4.46	9.7/16.2	240/248	220/229	3.95/4.20	-1.8/8.5
11/10/64-12/10/64	30	0.1257	196/243	182/213	4.39/6.24	17.8/35.9	243/253	216/244	3.59/4.56	-20.9/37.8
11/5/64-12/20/64	45	0.1759	167/224	157/199	5.37/8.16	14.9/30.4	226/259	189/257	3.41/5.54	-32.1/50.1
12/28/66-1/12/67	15	0.0962	189/201	149/159	5.58/6.25	-23.1/-14.3	202/212	159/171	4.87/5.53	-29.3/-17.8
12/21/66-1/20/67	30	0.1120	173/206	138/155	5.86/7.23	-27.1/-9.3	203/220	152/182	4.38/5.98	-37.7/-14.6
12/13/66-1/27/67	45	0.1397	158/203	127/164	5.25/8.41	-24.3/-5.6	194/227	148/194	4.01/6.23	-44.6/-8.4
2/24/69-3/11/69	15	0.092	165/178	108/119	4.92/5.88	-51.9/-43.6	180/189	115/129	4.34/5.22	-56.1/-46.7
2/16/69-3/18/69	30	0.1049	151/181	98/128	4.40/6.91	-55.1/-38.1	183/201	109/145	3.79/5.70	-63.3/-43.3
2/9/69-3/26/69	45	0.1235	140/193	92/151	3.66/7.86	-51.5/-34.3	188/212	109/163	3.62/5.72	-68.9/-44.2
5/16/71-5/31/71	15	0.0815	186/212	130/175	2.83/2.99	-27.2/-15.6	214/230	160/191	2.82/3.04	-22.5/-6.7
5/8/71-6/7/71	30	0.0896	164/201	106/169	2.86/3.64	-30.0/-18.0	203/240	137/208	2.84/3.24	-29.5/5.8
5/1/71-6/15/71	45	0.1033	147/208	90/188	2.91/4.52	-30.6/-13.3	208/242	135/223	2.88/3.51	-33.6/16.2
7/21/73-8/5/73	15	0.1507	176/186	154/169	3.22/3.53	23.8/38.0	202/209	184/206	2.71/2.97	30.9/35.6
7/13/73-8/12/73	30	0.166	159/185	132/184	2.96/4.26	19.9/27.8	204/223	176/233	2.54/3.11	2.2/42.6
7/5/73-8/19/73	45	0.1903	143/194	114/185	2.96/5.10	16.9/30.9	199/235	153/259	2.45/3.44	28.1/49.1
9/7/75-9/22/75	15	0.1964	186/226	191/209	4.17/4.68	41.7/47.0	216/226	227/254	3.10/3.68	47.3/54.9
8/31/75-9/30/75	30	0.2237	165/194	164/215	4.01/5.78	37.2/47.5	215/245	214/285	2.62/4.03	42.4/62.6
8/23/75-10/7/75	45	0.2683	147/192	143/198	4.64/6.99	33.7/47.3	212/264	198/315	2.39/4.46	45.0/69.7
10/11/77-10/26/77	15	0.1806	198/216	209/230	4.54/5.33	42.5/50.8	223/247	232/275	3.10/4.42	48.5/57.7
10/4/77-11/3/77	30	0.2122	176/207	182/240	4.18/6.66	38.0/47.6	226/273	228/308	2.49/4.59	45.7/66.0
9/30/77-11/4/77	45	0.2376	164/306	170/339	2.46/7.44	25.1/47.6	222/309	218/340	2.51/4.95	12.2/70.2
VENUS										
8/13/62-8/28/62	15	0.09	108/122	54/59	5.40/5.92	-7.8/-0.6	110/123	57/62	5.20/5.58	-1.5/5.9
8/4/62-9/3/62	30	0.0985	101/127	50/59	5.41/6.49	-13.5/-1.7	106/130	56/66	4.98/5.63	0.2/12.6
7/26/62-9/9/62	45	0.112	94/135	47/57	5.62/7.18	-18.0/-4.2	104/138	53/69	4.78/5.79	-4.1/18.3
3/22/64-4/6/64	15	0.128	104/115	55/60	6.06/6.82	-3.6/0.7	108/119	60/66	5.39/6.12	-11.1/-5.2
3/14/64-4/13/64	30	0.142	96/127	51/59	6.30/7.74	-3.6/5.8	106/125	57/72	4.82/6.50	-17.1/-5.7
3/5/64-4/19/64	45	0.1645	88/128	48/60	6.19/8.71	-1.2/9.8	102/132	55/78	4.34/6.79	-22.2/-3.8
11/5/65-11/20/65	15	0.1370	99/108	54/58	5.05/5.75	9.2/13.7	111/115	60/69	3.73/4.70	13.9/19.0
10/27/65-11/26/65	30	0.1537	91/115	48/63	4.33/6.94	4.9/15.8	111/121	55/81	3.02/5.49	9.6/24.1
10/19/65-12/3/65	45	0.1750	84/121	45/89	2.99/7.92	2.0/16.7	118/126	51/96	2.99/6.03	7.2/27.8
6/8/67-6/23/67	15	0.0842	128/144	81/91	2.81/3.42	-18.5/9.1	133/146	93/96	2.96/4.90	-16.0/35.9
5/30/67-6/29/67	30	0.1065	110/127	60/93	3.31/5.15	-23.7/15.2	127/145	72/98	2.88/5.61	-27.3/44.4
5/21/67-7/5/67	45	0.1344	96/132	51/96	3.45/6.96	-27.4/20.0	122/146	61/100	3.13/6.27	-33.7/48.0
1/4/69-1/19/69	15	0.0805	119/132	66/69	4.53/4.73	2.2/8.8	123/134	70/74	4.49/4.62	-8.4/-0.4
12/27/68-1/26/69	30	0.0894	111/140	61/68	4.45/5.22	2.5/15.4	119/141	68/78	4.44/4.88	-16.3/3.5
12/17/68-1/31/69	45	0.1035	103/148	56/70	4.26/5.92	-0.9/20.3	113/149	67/82	4.39/5.26	-23.1/3.7
8/9/70-8/24/70	15	0.088	109/120	54/58	5.51/5.88	-8.2/-2.8	112/124	59/62	5.17/5.44	1.8/6.3
8/1/70-8/31/70	30	0.0965	102/126	51/58	5.47/6.42	-13.6/-2.7	107/131	57/66	4.98/5.57	1.5/12.4
7/23/70-9/6/70	45	0.1105	95/134	48/54	5.87/7.13	-18.3/-8.1	109/139	55/70	4.79/5.73	0/18.6
MERCURY										
11/16/67-12/1/67	15	0.4415	99/112	125/130	15.04/15.62	-15.6/-3.9	99/113	130/132	15.02/15.44	-21.6/-16.4
11/11/67-12/11/67	30	0.5685	88/118	114/131	13.52/20.15	-18.6/12.3	91/131	128/156	13.78/17.81	-39.0/12.3
11/5/67-12/20/67	45	0.8195	76/114	103/124	16.88/27.96	-14.9/11.2	87/119	121/144	15.10/20.07	-48.2/22.0
11/8/68-11/23/68	15	0.5902	91/103	127/139	13.90/16.74	-13.7/7.0	94/105	134/147	12.52/16.93	-43.8/8.0
10/31/68-11/30/68	30	0.7825	81/105	112/145	13.93/25.00	-23.3/9.3	87/107	123/151	13.81/18.86	-51.2/16.7
JUPITER										
12/27/70-1/11/70	15	0.7882	810/1035	641/866	5.72/6.65	-7.7/4.4	902/1043	633/876	5.72/6.00	-16.1/8.6
12/21/70-1/20/70	30	0.8612	675/1077	638/940	5.74/8.69	-7.1/4.7	820/1122	636/920	5.81/6.64	-24.6/16.9

^aReproduction of this table was authorized by the Jet Propulsion Laboratories, Pasadena, Calif.^bAll double values are min/max values for the specified launch period.

spacecraft with a particular injection energy can fly a variety of missions.

Also listed are the following, where t_L is the launch period, t_f the flight time, S_{com} the communication distance at the time of planetary encounter, V_{hss} the hyperbolic excess velocity of the vehicle with respect to the target planet, and δ_θ the declination of the geocentric asymptote, which places restrictions on the ascent trajectory. The minimum/maximum values of these parameters bracket the interval containing the value for any given launch within the time interval.

The boosters in this study are compared in Fig. 1 by generating curves of payload vs $2E/m_1$. The actual terminal velocity V of the vehicle is given by⁴:

$$(V + V_L)/g = \sum_{j=1}^n I_{spj} \ln(W_{ij} + P)/(W_{fj} + P) \quad (3)$$

Note that the "payload" P includes any required guidance equipment and other support subsystems in addition to the scientific payload. A computer program based upon Eqs. (2) and (3) was used to find $2E/m_1$ as a function of payload weight for Atlas-Centaur, three-stage Saturn 1B, and Saturn 5 boosters, using the specifications in Table 2 as inputs. The results appear in Fig. 1 for $V_L =$ to 1524 m/sec (5 kft/sec). The actual value of V_L will vary slightly for each booster and mission, but this value is within $\pm 10\%$ for planetary missions.⁵ For example, for the three-stage Saturn 1B with a 5000-lb payload, substitution of the appropriate I_{sp} , W_i , and W_f for each stage from Table 2 into Eq. (3) gives $V + V_L = 13,564$ m/sec. Using $V_L =$ to 1524 m/sec, $V = 12,040$ m/sec. Substituting into Eq. (2), $2E/m_1 = 0.234(10^8)\text{m}^2/\text{sec}^2$.

The planning sequence for any planetary mission can be summarized in the following four steps: 1) choose a planet and a mission objective (flyby, orbiter, etc.); 2) choose transfer characteristics, including the launch date and the required injection energy from Table 1; 3) determine the payload weight based on the objectives; and 4) choose a suitable booster. Assuming that the destination and the primary mission objectives are fixed, tradeoffs among booster capabilities, payload weight, launch date, and secondary mission objectives must be made so that the final payload weight conforms to the capability of the boosters available at the chosen launch time. The choice of a launch date involves tradeoffs among the tabulated transfer characteristics. Short flight time is desirable to minimize the probability of a failure in the spacecraft and the susceptibility to injection errors. For orbiter and lander missions, it is desirable to minimize the hyperbolic excess speed to permit the heaviest possible payload. However, the minimum values of V_{hss} do not correspond with the minimum values of $2E/m_1$, so a compromise must be made. Finally, δ_θ places restrictions on the ascent trajectory; values between $\pm 34^\circ$ must be chosen for launches for the Atlantic Missile Range.

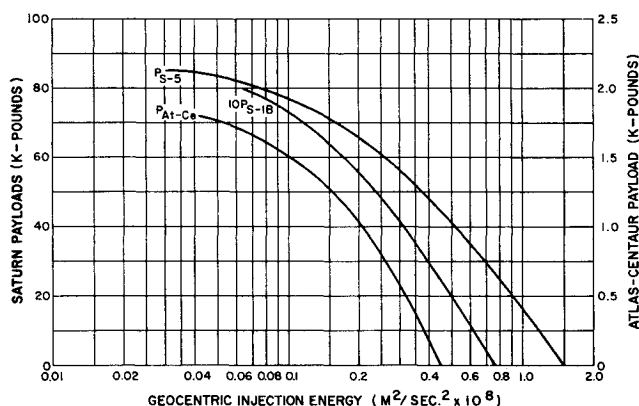


Fig. 1 Payload vs geocentric injection energy for Atlas-Centaur, three-stage Saturn 1B, and Saturn 5.

Table 2 Booster specifications

Booster	Stage	I_{sp} , sec	W_i , klb	W_f , klb
Atlas-Centaur	1	257	292	44
	2	420	32	3
Saturn 1-B	1(S-1)	257	1250	404
	2(S-4B)	420	285	54.7
	3(S-6)	420	26.7	6.4
Saturn 5	1(S-1C)	257	5951	1551
	2(S-2)	420	1263	333
	3(S-4B)	420	258	28

Example

It is desired to launch a flyby probe to Mars at an appropriate time during 1966 or 1967. Table 1 shows that a launch between December 28, 1966 and January 12, 1967 would require $2E/m_1 = 0.0962(10^8)\text{m}^2/\text{sec}^2$, and δ_θ for this trajectory is within the $\pm 34^\circ$ required for launch at the Atlantic Missile Range. Payload capabilities for this value of $2E/m_1$ are obtained from Fig. 1 as follows: Atlas-Centaur, 1510 lb; Saturn 1B, 7400 lb; Saturn 5, 76,000 lb.

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Orbital Elements from Doppler Tracking of Three Satellites

ROBERT R. NEWTON*

Applied Physics Laboratory, The Johns Hopkins University, Silver Spring, Md.

THREE satellites, 1961 $\alpha 1$, 1961 $\alpha \eta 1$, and 1962 $\beta \mu 1$, have each transmitted four coherent frequencies controlled by highly stable oscillators and have been tracked by Doppler methods. The orbital elements resulting from this tracking are of research interest in two different ways. First, their secular and long-term periodic perturbations can be analyzed to yield equations of condition connecting the zonal harmonics in the earth's gravitational field. Second, because of the unique nature of the radio signals from these satellites, they have been used in studies of radio propagation through the ionosphere and troposphere and in studies of the reflections of radio signals from the earth's surface.

This paper presents three tables of the orbital elements of these satellites which are adequate for either of these types of

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* Supervisor, Space Research and Analysis Group. Member AIAA.